

Differential equations in Matlab/Simulink

- I) Solve the following: $dz(t)/dt=t*e^{-z}$, $z(0)=-2$
Note that t is a linearly increasing signal with slope 1.
I have written the exponential function in the block **Matlab function**.
The initial condition is written in the block **Integrator**.
In Figur Ib you can see the solution !

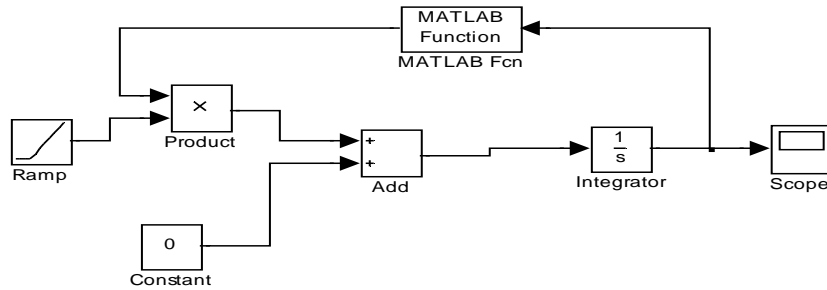


Figure Ia

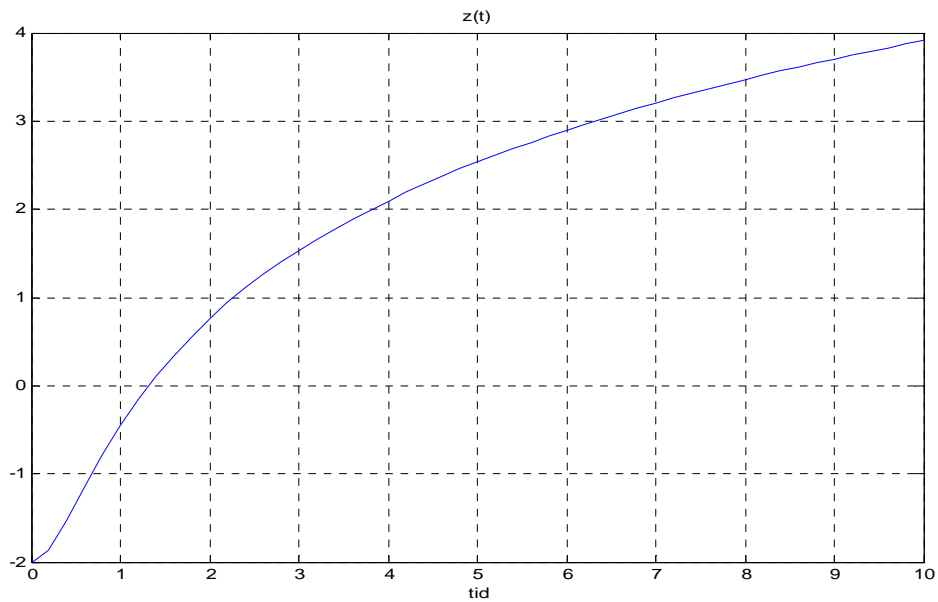


Figure Ib

II) Solve $dz/dt = z^2 - z^3 + \sin(t)$, $z(0) = 0.5$
 The differential equation in Simulink is implemented like Figure IIa.
 The solution is shown in Figure IIb.

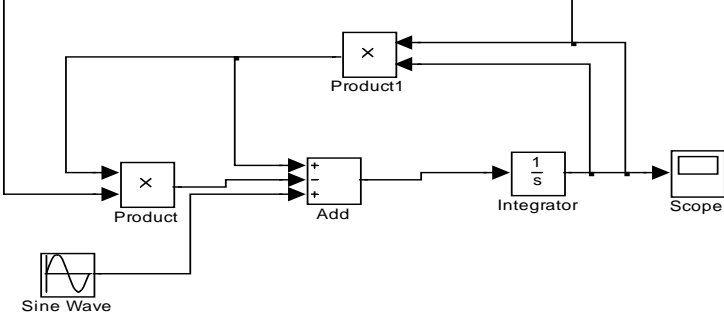


Figure IIa

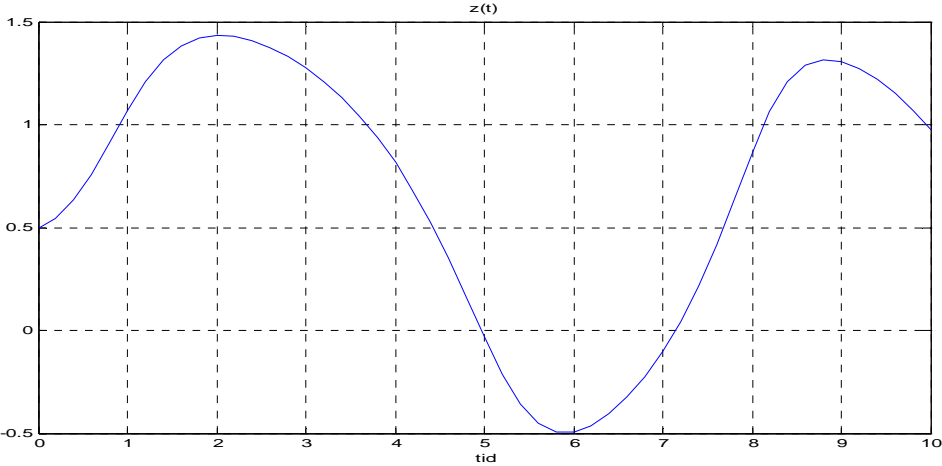


Figure IIb

III) Solve $d^2z(t)/dt^2 - dz(t)/dt + 4z(t) = t \cdot \sin(t)$, $z(0)=1$, $dz(0)/dt=-3$
 What kind of strategy to use ? I suggest that you eliminate everything on one side of the equality sign except for the time differentiation of the highest order.
 Then formulate the whole differential equation around the **Add** block.
 The initial condition $dz(0)/dt$ is inserted into the left integrator and $z(0)$ in the right. See the solution in Figure IIIb.

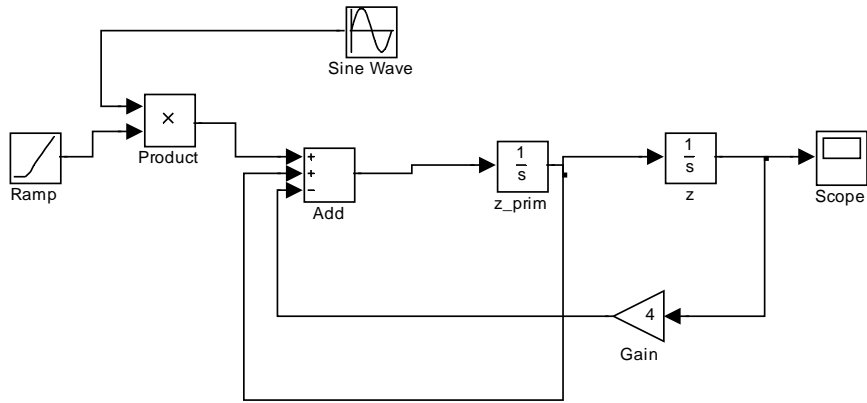


Figure IIIa

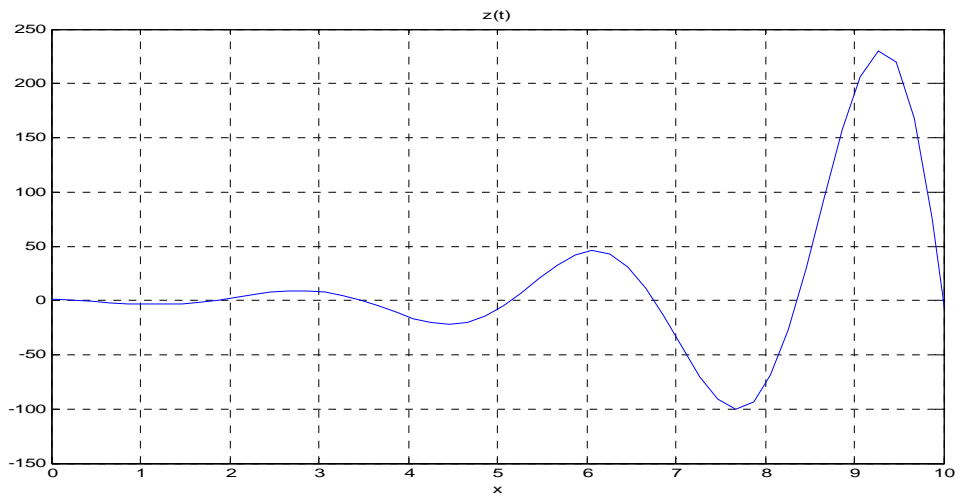


Figure IIIb

IV) Solve: $d^2z(t)/dt^2 - 2dz(t)/dt + 10z(t) * dz(t)/dt = 10 * e^{-0.1 * \cos(2t)}$
 With initial conditions: $z(0) = -1$, $dz(0)/dt = 1$
 Sine Wave can be changed to a cosine wave by a phase shift of 90° .
 In the Matlab function we have written the following: $10 * e^{-0.1t}$.
 The initial conditions are inserted into the integrators.
 The condition $dz(0)/dt$ is in the left integrator and $z(0)$ in the right.
 See the solution in Figure IVb !

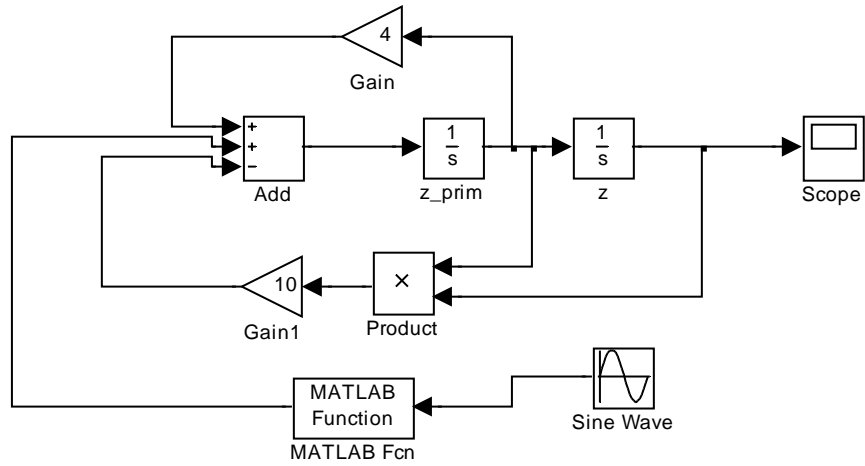


Figure IVa

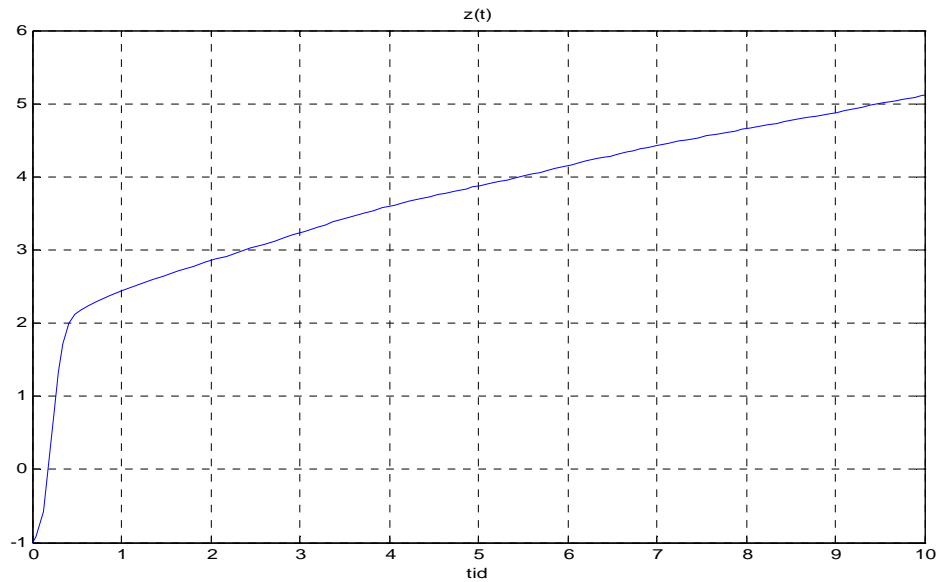


Figure IVb